

The electrical power dissipated by a resistor is given by  $P = I^2 R$ . It is also given by  $P = (\Delta V)^2 / R$ . So is the power really proportional to  $R$  or to  $1/R$  or is neither really true? Discuss thoroughly.

Good discussion of relationships

**These given equations describing electrical power dissipated by a resistor are neither really true.**  $P = I^2 R$  can be derived from the relationship determined in lab  $P = (I) \Delta V$ , where  $\Delta V = IR$ . Therefore,  $P = I^2 R$ . The equation for voltage can be manipulated so that the current ( $I$ ) is equal to the voltage divided by the resistance. Using this value for  $I$  in the equation for power,  $P = (\Delta V / R)(\Delta V)$  or  $(\Delta V)^2 / R$ . **The current and the change in voltage are referring to two separate entities.** Therefore the quantities  $[(\Delta V)^2 / R]$  and  $(I^2 R)$  are two separate entities as well. **So, it is not really true to say that  $P$  is either proportional or inversely proportional to  $R$  because it is ignoring the differences between electric potential and current.**

Truth is a practical issue here:

**Neither is really true.** When we set these two expressions equal to each other we get

$$I^2 R = (\Delta V^2) / R \quad \text{From this we can then get } I^2 R^2 = \Delta V^2$$

If we then take the square root of each side, we get

$$\Delta V = IR \quad \text{which is Ohms Law}$$

As a result, **the power dissipated is not necessarily proportional or inversely proportional but is dependent upon the practicality and ease of use for the equation.**

Key question to ask always practically: what remains constant?

Power can be proportional to either  $R$  or  $1/R$  depending on the situation. **If the current ( $I$ ) is a constant value**, then  $P$  will be proportional to  $R$  as  $I^2$  will stay the same. **If the potential difference ( $\Delta V$ ) is held constant**, then power would be proportional to  $1/R$  as the numerator would stay the same.

Unlike the new, compact fluorescent bulbs, an ordinary light bulb is basically a thin wire filament that acts as a simple resistor. Estimate the resistance of such a bulb using some common numbers from ordinary household experience that previously may not have meant much to you. And look at the equations I gave you in the first question.

Straightforward application of the relevant formulas, clear algebra

Lets say an ordinary bulb is  $P=80\text{ W}$ ,  $\Delta V=120\text{ V}$

$$P = (\Delta V)^2 / R$$

$$R = (\Delta V)^2 / P$$

$$= (120\text{V})^2 / 80\text{ W}$$

$$= 14400\text{ V}^2 / 80\text{ W}$$

appr. = less than 200 ohms = 175 ohms

dp - note easier way to do math

$$R = (\Delta V)^2 / P$$

$$= (120\text{V})^2 / 80\text{ W}$$

$$= (120\text{V} / 80\text{W}) 120\text{V}$$

$$= (1.5\text{V/W}) 120\text{V} = 180\text{ ohm}$$

But what about the units?

One of the lightbulbs I use for a lamp is **70 watts** (or something like that, it doesn't really matter). This is powered by an outlet that provides a **110 V potential drop**. As power  $P = (\Delta V)^2 / R$ , then  $R = (\Delta V)^2 / P$ . So:

$$R = (\Delta V)^2 / P = (110\text{ V})^2 / (70\text{ W}) = (10000/70)\text{ V}^2/\text{W}$$

So, approximately,

$$R = (10000/50)\text{ V}^2/\text{W}$$

$$= (1000/5)\text{ (J/C)}^2/(\text{J/s})$$

$$= 200\text{ (J*s)} / (\text{C}^2)$$

$$= 200\text{ V/A} = 200\text{ ohms}$$

So, the wire filament has a resistance of around 200 ohms or so.

Charge is for a capacitor as what is for a resistor?

- a. energy
- b. power
- c. current
- d. potential